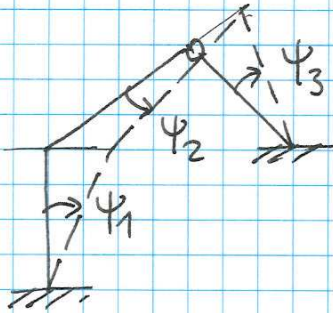


$$S = \frac{1}{100} \frac{EI}{L^2}$$

$$\sigma_1 = 0,4$$

Obliczy:  $M_A$



$$\begin{aligned} \psi_1 &= \psi \\ \psi_2 &= -\frac{4}{7} \psi \\ \psi_3 &= \frac{16}{21} \psi \end{aligned}$$

$$\begin{cases} \phi_1^1 + \phi_1^2 = 0 \\ (\phi_A^1 + \phi_1^1) \bar{\varphi} + \phi_1^2 \left(-\frac{4}{7} \bar{\varphi}\right) + \phi_B^3 \frac{16}{21} \bar{\varphi} + S \cdot 4L \cdot \psi \cdot \bar{\varphi} - 4ql \cdot 3L \cdot \frac{16}{21} \bar{\varphi} + 8ql^2 \left(-\frac{4}{7} \bar{\varphi}\right) = 0 \end{cases}$$

$$\phi_A^1 = \frac{EI}{4L} [\beta(\sigma_1) \psi_1 - \theta(\sigma_1) \psi]$$

$$\phi_1^1 = \frac{EI}{4L} [\alpha(\sigma_1) \psi_1 - \theta(\sigma_1) \psi]$$

$$\phi_1^2 = \frac{3EI}{5L} \left[ \psi_1 + \frac{4}{7} \psi \right] + 4ql^2$$

$$\phi_B^3 = \frac{3EI}{372L} \left( -\frac{16}{21} \psi \right)$$

$$\frac{EI}{L} \begin{bmatrix} \frac{1}{4} \alpha(0,4) + \frac{3}{5} & -\theta(0,4) + \frac{4}{7} \cdot \frac{3}{5} \\ -\theta(0,4) + \frac{4}{7} \cdot \frac{3}{5} & \frac{1}{2} \theta(0,4) + \frac{48}{245} + \frac{256}{441\sqrt{2}} - 4\sigma^2 \end{bmatrix} \begin{bmatrix} \psi_1 \\ \psi \end{bmatrix} + \begin{bmatrix} 4 \\ 16 \end{bmatrix} ql^2 = 0$$

$\sigma = 0,1$

$$\psi_1 = -7,52 \frac{ql^3}{EI}$$

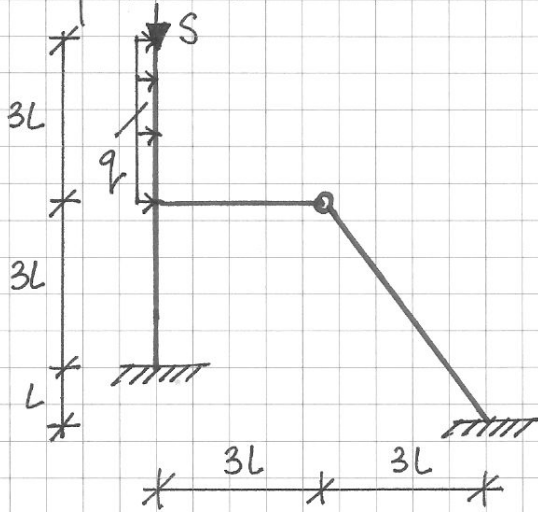
$$\psi = -6,93 \frac{ql^3}{EI}$$

$$\phi_A^1 = 6,6 ql^2$$

Kolokwium z MK2, 1.2, r.ak. 2013/14

Zapisać układ równań metody przemieszczeń  $EJ = \text{const.}$

$$S = \frac{1}{100} \frac{EJ}{L^2}$$



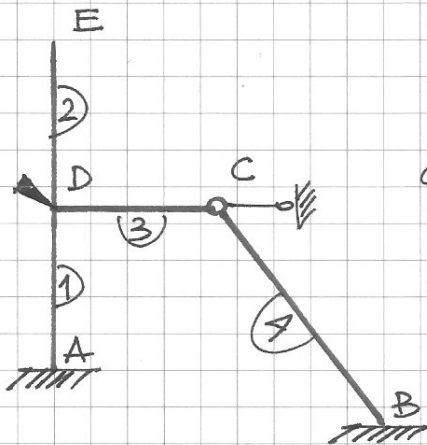
Wartości dużych sił osiowych i parametrów  $\sigma^{(k)}$  w prętach:

$$S^{(1)} = S \quad \sigma^{(1)} = 0,3$$

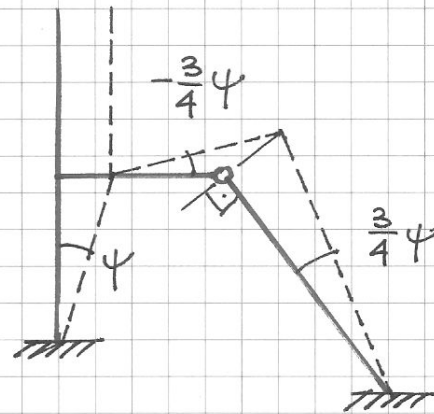
$$S^{(2)} = S \quad \sigma^{(2)} = 0,3$$

Schemat geometrycznie wyznaczalny:

Plan przesunąć:



$$q = \begin{bmatrix} \varphi_D \\ \psi \end{bmatrix}$$



Równania równowagi:

$$\Phi_D^{(1)} + \Phi_D^{(2)} + \Phi_D^{(3)} = 0$$

$$\begin{aligned} [\Phi_A^{(1)} + \Phi_D^{(1)}] \cdot \bar{\psi} + \Phi_D^{(3)} \cdot \left(-\frac{3}{4} \bar{\psi}\right) + \Phi_B^{(4)} \cdot \frac{3}{4} \bar{\psi} \\ + S \cdot 3L \cdot \psi \cdot \bar{\psi} \\ + q \cdot 3L \cdot 3L \cdot \bar{\psi} = 0 \end{aligned}$$

Wzory transformacyjne:

$$\Phi_A^{(1)} = \frac{EJ}{3L} [\beta(0,3) \varphi_D - \gamma(0,3) \psi]$$

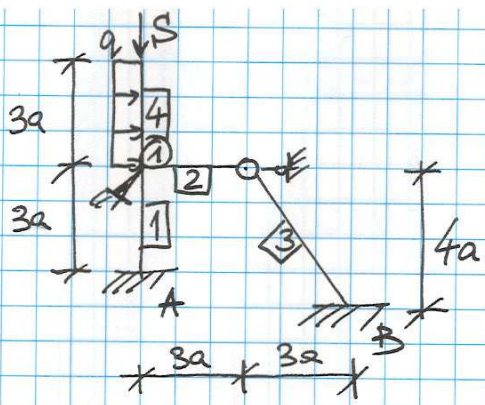
$$\Phi_D^{(1)} = \frac{EJ}{3L} [\alpha(0,3) \varphi_D - \gamma(0,3) \psi]$$

$$\Phi_D^{(2)} = \frac{EJ}{3L} [\alpha'''(0,3) \varphi_D] - \gamma'''(0,3) q (3L)^2$$

$$\Phi_D^{(3)} = \frac{3EJ}{3L} \left[ \varphi_D + \frac{3}{4} \psi \right]$$

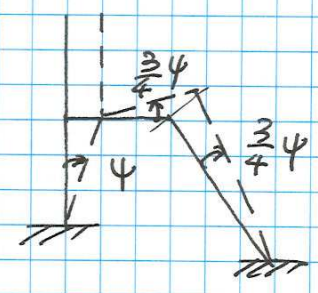
$$\Phi_B^{(4)} = \frac{3EJ}{5L} \left[ -\frac{3}{4} \psi \right]$$

Kol 1.2  
8.05.2014 r.



$$S' = \frac{1}{100} \frac{EI}{a^2}$$

$$M_A = ?$$



$$\sigma_4 = 0.1$$

$$\sigma_1 = 0.3$$

$$\sigma_4 = 0.3$$

$$\int \phi_1^1 + \phi_1^2 + \phi_1^4 = 0$$

$$\left[ (\phi_A^1 + \phi_1^1) \bar{\Psi} + \phi_1^2 \left(-\frac{3}{4} \bar{\Psi}\right) + \phi_B^3 \left(\frac{3}{4} \bar{\Psi}\right) + S \cdot 3a \cdot \Psi \cdot \bar{\Psi} + 3qa \cdot 3a \cdot \bar{\Psi} = 0 \right]$$

$$\phi_A^1 = \frac{EI}{3a} [\beta(\sigma_1) \varphi_1 - \theta(\sigma_1) \Psi]$$

$$\phi_B^3 = \frac{3EI}{5a} \left(-\frac{3}{4} \Psi\right)$$

$$\phi_1^1 = \frac{EI}{3a} [\alpha(\sigma_1) \varphi_1 - \theta(\sigma_1) \Psi]$$

$$\phi_1^4 = \frac{EI}{3a} \alpha'''(\sigma_4) \varphi_1 - \gamma''(\sigma_4) q \cdot (3a)^2$$

$$\phi_1^2 = \frac{3EI}{3a} \left[\varphi_1 + \frac{3}{4} \Psi\right]$$

$$\frac{EI}{a} \begin{bmatrix} 2.2983 & -1.247 \\ -1.247 & 4.864 \end{bmatrix} \begin{bmatrix} \varphi_1 \\ \Psi \end{bmatrix} = \begin{bmatrix} 4.605 \\ 9 \end{bmatrix} qa^2$$

$$\varphi_1 = 3.49 \frac{qa^3}{EI} \quad \Psi = 2.75 \frac{qa^3}{EI}$$

$$M_A = \phi_A^1 = -3.15 qa^2$$