

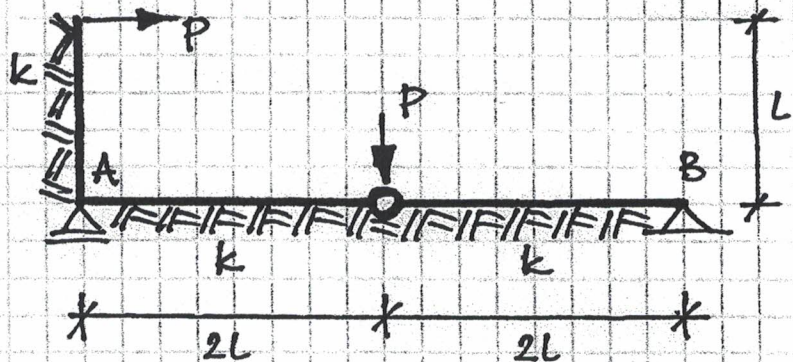
Egzamin z Mechaniki Konstrukcji (MK3 IPB), 8.09.2019
studia niestacjonarne

NAZWISKO, Imię			
nr albumu	grupa (IPB / BZ)	tryb studiów (ST / NST)	
ocena zadania 1	ocena zadania 2	ocena zadania 3	ocena egzaminu pisemnego

Zadanie 1.

Oblicz poziome i pionowe składowe reakcji podpór A (podpora przesuwna) i B (podpora nieprzesuwna) ramy z rys.1.

$$EJ = \text{const.}, k = 0,9604 \frac{EJ}{l^4}.$$



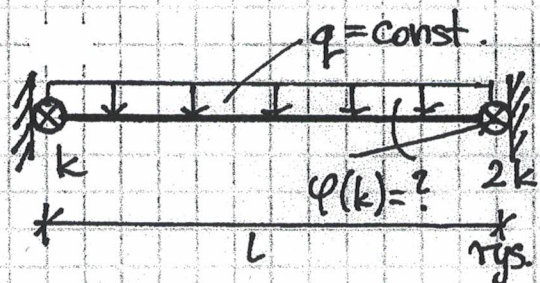
rys. 1

Zadanie 2.

Oblicz wartość $\varphi(k)$ w ramie z rys. 2

dla $k = \frac{EJ}{l}$, $k = 5 \frac{EJ}{l}$, $k = 20 \frac{EJ}{l}$, $k = +\infty$.

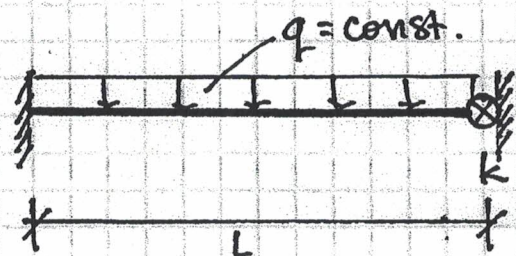
Uwaga: Podpory mają różne współczynniki sprężystości ze względu na obrót.



rys. 2

Zadanie 3.

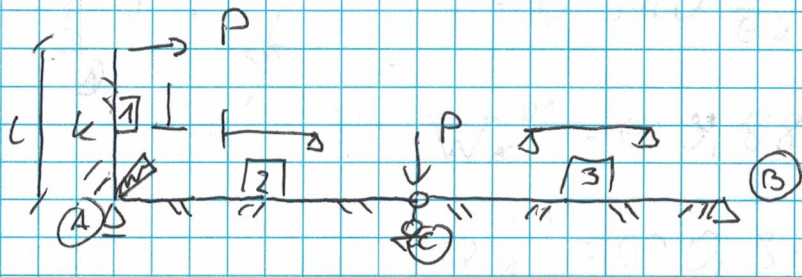
Wyprowadź równanie linii ugięcia belki z rys. 3.



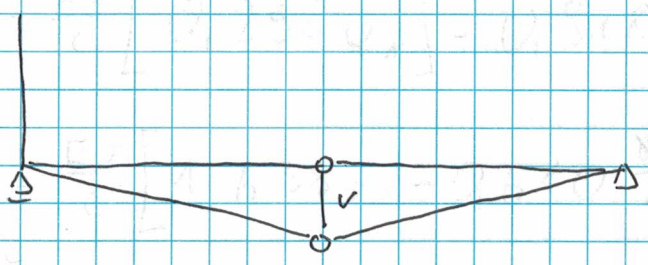
rys. 3

Zadanie 1

$$q_1 = \begin{bmatrix} u_A \\ \frac{v}{L} \end{bmatrix}$$



PP



Przet	w^*	w^*	u	Δ
1	0	0	0	0,7
2	0	v	0	1,4
3	v	0	0	1,4

RR.

$$\begin{cases} \Phi_1^1 + \Phi_1^2 = 0 \\ \ominus(W_c^2 \bar{v} + W_c^3 \bar{v}) + P\bar{v} = 0 \end{cases}$$

$$\frac{EJ}{L} \begin{bmatrix} 1,936 & -0,610 \\ -0,610 & 1,399 \end{bmatrix} \begin{bmatrix} u_A \\ \frac{v}{L} \end{bmatrix} = \begin{bmatrix} 0,918 \\ 1 \end{bmatrix} PL$$

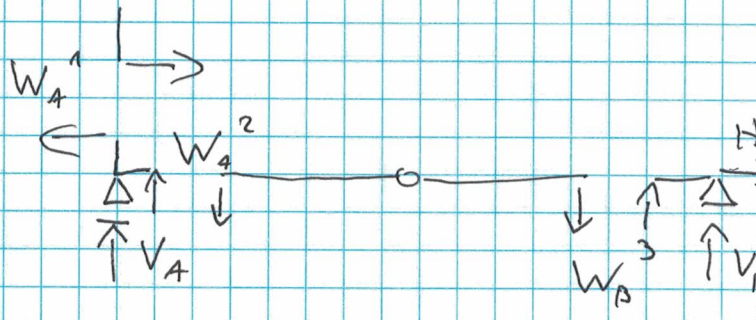
$$u_A = 0,810 \frac{PL}{EJ}$$

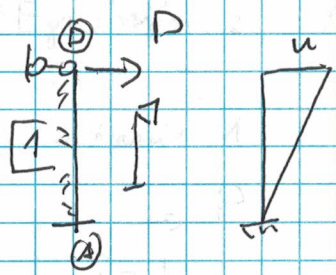
$$\frac{v}{L} = 1,068 \frac{PL^2}{EJ}$$

$$V_A = \ominus W_A^2 = \ominus 0,726 P$$

$$V_B = \ominus W_B^3 = \ominus 0,286 P$$

$$H_B = \ominus W_A^1 = 0,525 P$$





$$-(\bar{W}_D^{01} \bar{u}) + P\bar{u} = 0$$

$$\frac{u}{l} = 0,310 \frac{Pl^2}{EI}$$

$$\bar{W}_A^{01} = \ominus 0,889P$$

$$\bar{\Phi}_A^{01} = \ominus 0,818Pl$$

$$\bar{\Phi}_A^1 = \frac{EI}{l} [0,298 \varphi_A] - 0,818Pl$$

$$\bar{\Phi}_A^2 = \frac{EI}{l} [1,638 \varphi_A - 0,610 \frac{u}{l}]$$

$$\bar{W}_C^2 = \frac{EI}{l^2} [\ominus 0,610 \varphi_A + 0,813 \frac{u}{l}]$$

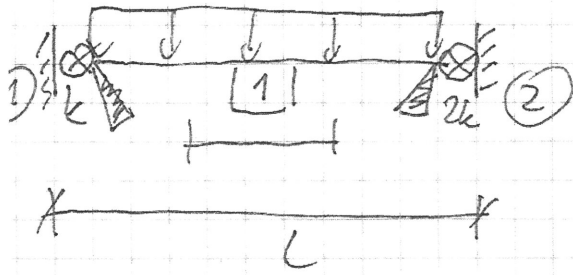
$$\bar{W}_C^3 = \frac{EI}{l^2} [0,586 \frac{u}{l}]$$

$$\bar{W}_A^1 = \frac{EI}{l^2} [0,449 \varphi_A] \ominus 0,889P$$

$$\bar{W}_A^2 = \frac{EI}{l^2} [1,064 \varphi_A \ominus 0,128 \frac{u}{l}]$$

$$\bar{W}_B^3 = \frac{EI}{l^2} [\ominus 0,268 \frac{u}{l}]$$

Zadanie 2



$$q_1 = \begin{Bmatrix} u_1 \\ u_2 \end{Bmatrix}$$

$$Q_1 = u_1 k$$

$$Q_2 = -u_2 \cdot 2k$$

RR:

$$\Phi_1^1 + Q_1 = 0$$

$$\Phi_1^1 = \frac{EJ}{L} [4u_1 + 2u_2] - \frac{1}{12} qL^2$$

$$\Phi_2^1 + Q_2 = 0$$

$$\Phi_2^1 = \frac{EJ}{L} [2u_1 + 4u_2] + \frac{1}{12} qL^2$$

$$\frac{EJ}{L} \begin{bmatrix} 4+k & 2 \\ 2 & 4+2k \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \begin{bmatrix} \frac{1}{12} \\ -\frac{1}{12} \end{bmatrix} qL^2$$

$$q(k) = u_2 = - \frac{6+k}{24(6+6k+k^2)} \frac{qL^3}{EJ}$$

$$q\left(\frac{EJ}{L}\right) = - \frac{7}{312} \frac{qL^3}{EJ}$$

$$q\left(5\frac{EJ}{L}\right) = - \frac{11}{1464} \frac{qL^3}{EJ}$$

$$q\left(20\frac{EJ}{L}\right) = - \frac{13}{6312} \frac{qL^3}{EJ}$$

$$q(\infty) = 0$$